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Forming Mercury from Excited Initial Conditions

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Abstract

Mercury is notoriously difficult to form in Solar System simulations, due to its small mass and iron-rich composition. Smooth particle hydrodynamics simulations of collisions have found that a Mercury-like body could be formed by one or multiple giant impacts, but due to the chaotic nature of collisions, it is difficult to create a scenario where such impacts will take place. Recent work has found more success forming Mercury analogues by adding additional embryos near Mercury's orbit. In this work, we aim to form Mercury by simulating the formation of the Solar System in the presence of the giant planets Jupiter and Saturn. We test out the effect of an inner disk of embryos added on to the commonly used narrow annulus of initial material. We form Mercury analogues with core-mass fractions (CMFs) > 0.4 in $\sim 10\%$ of our simulations, and twice that number of Mercury analogues form during the formation process but are unstable and do not last to the end of the simulations. Mercury analogues form at similar rates for both disks with and without an inner component, and most of our Mercury analogues have lower CMFs than that of Mercury, ~ 0.7 , due to significant accretion of debris material. We suggest that a more in-depth understanding of the fraction of debris mass that is lost to collisional grinding is necessary to understand Mercury's formation, or some additional mechanism is required to stop this debris from accreting.

Unified Astronomy Thesaurus concepts: Mercury (planet) (1024); Solar system formation (1530); Collisional processes (2286); Solar system terrestrial planets (797)

1. Introduction

Mercury has long been set apart from the other terrestrial Solar System planets due to its orbit, diminutive size, and disproportionately large iron core. Many possible explanations have been proposed to explain its existence. The most prominent theory is that Mercury's high core-mass fraction (CMF; 0.69–0.77; Hauck et al. 2013) and high eccentricity (0.2) originated from a collision with another planet or embryo during the giant impact phase near the end of its formation (Benz et al. 1988). The details of the collision vary from a head-on, high-speed impact (Benz et al. 2007) to a "hit-and-run" impact where Mercury is the impactor (Asphaug & Reufer 2014). In the latter scenario, Mercury hits a larger body at a glancing angle, shearing off much of the mantle material from its outer edges and leaving behind a planet enriched in core material. One difficulty with this scenario is that it requires high impact velocities that are thought to be unlikely during Solar System formation. Thus, it is more likely that Mercury formed from multiple subsequent collisions, allowing each collision to occur at more reasonable impact velocities (Chau et al. 2018; Jackson et al. 2018; Clement et al. 2023a). Another theory for Mercury's formation is that it formed from iron-rich material that preferentially exists at, or drifts into, the close-in semimajor axes where it formed (Weidenschilling 1978; Aguichine et al. 2020; Johansen & Dorn 2022). Hyodo et al. (2021) suggested that the iron-rich material that forms Mercury could

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be generated by inner planetesimals that are stripped of their mantles as they collide with each other. This idea of Mercury forming from iron-rich material combines well with the collisional theory, as it may provide part of the iron enrichment necessary to form Mercury, requiring fewer, or less destructive, collisions to achieve the remaining iron enrichment.

Previously, it was impossible to properly test the collisional theory in simulations of Solar System formation because the Nbody codes used to simulate planet formation treated all collisions as perfect mergers. Multiple N-body codes have been updated over the last 10 years to include more detailed collisional outcomes, including the hit-and-run necessary for one of the collisional theory's possible Mercury formation pathways. Still, some works (i.e., Lykawka & Ito 2019; Fang & Deng 2020; Franco et al. 2022) that aim to form Mercury do not make use of these codes with more detailed collisional outcomes. These updates slow simulations down significantly, and some previous works (Chambers 2013; Walsh & Levison 2016) show that, overall, the differences in the final planet configurations and accretion timescales are not statistically significant. These studies suggest that including collisional details is not worth the extra computational time required. In contrast, however, more recent works (e.g., Haghighipour & Maindl 2022; Scora et al. 2022) have found that detailed collisional outcomes can make an impact on dynamics and compositions of final planets, in particular in an excited environment where collisional velocities are high enough to generate significant masses of debris. More importantly, to properly test whether the collisional theory can explain Mercury's iron enrichment, collisions that are not perfect mergers are required. Thus, in this work we use an N-body code with a prescription for imperfect, debris-producing collisions to test the success of the collisional method in forming iron-rich Mercury analogs.

Simulations forming the terrestrial planets must focus on one stage of planet formation at a time, due to computational constraints. Here, we focus on the later stages of planet formation, where an initial disk of embryos grow into planets via giant impacts. The majority of previous work on this stage of formation has shown that certain conditions work best to reproduce the three larger terrestrial planets—Venus, Earth, and Mars. The initial disk of embryos produces the best Mars analogs when it begins as a truncated disk (typically between 0.7 and 1 or 1.2 au; Hansen 2009). These truncated initial disks may have been formed due to giant-planet migration (called the Grand Tack; Walsh et al. 2011; Walsh & Levison 2016), giantplanet instabilities (Tsiganis et al. 2005; Clement et al. 2018), or simply because planetesimals form in these smaller rings instead of a larger disk (Izidoro et al. 2021; Morbidelli et al. 2022). Some observational evidence seems to support an early giant-planet instability (Clement et al. 2023b), such as the timeline of the impacts on the Moon (Ogihara et al. 2018), and recent simulations suggest that the dispersal of the gas disk may trigger a giant-planet instability (Liu et al. 2022). However, there is some debate as to which scenario is the most in line with Solar System observations.

Most of this work constraining the details of the formation of the terrestrial planets has been based on the success of the simulations in forming analogs of the three larger terrestrial planets. In some cases, Mercury's formation was ignored altogether because of the limitations of the simulations. Most often, though, it was because simulations produce Mercury analogs infrequently, and those that are produced are often too massive and too close to Venus (Clement et al. 2019). This is true of both simulations with and without prescriptions for detailed collisional outcomes (Jacobson & Morbidelli 2014; Walsh & Levison 2016; Clement et al. 2019; Lykawka & Ito 2019).

Recently Clement et al. (2021, 2023a) and Clement & Chambers (2021) ran simulations of Mercury's formation with collisional fragmentation that improved the occurrence rates of Mercury analogs from <1% to 5%-10%, though they remained on average too massive. In all three cases, they added an inner disk component around Mercury's current orbit to help it form. Lykawka & Ito (2019) had previously added an inner disk component without including fragmentation and similarly found that it improves the rate of Mercury analogs (\sim 7%), though they did not consider Mercury's CMF. In this paper, we test the effect of an inner disk on the rate of forming Mercury in the presence of Jupiter and Saturn. Our treatment of debris, giant-planet configurations, and inner disk profiles differ from the works of Lykawka & Ito (2019), Clement & Chambers (2021), and Clement et al. (2021, 2023a), and we compare our results to theirs in Section 4.3. In Section 2, we outline and justify our initial conditions and how the simulations are run. Section 3 and Section 4 display and discuss the outcomes of these simulations, respectively. Finally, Section 5 discusses the most important takeaways from this study.

2. Methods

2.1. Initial Conditions

To test the effectiveness of added material interior to 0.7 au, we simulate formation starting from two different embryo

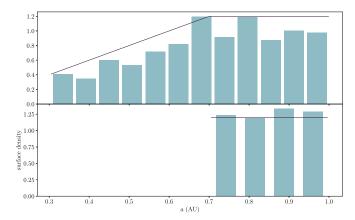


Figure 1. The surface density profiles of two runs (histogram in light blue), compared to the probability density they were drawn from (in black). Top: the profile for a "piecewise" distribution. Bottom: the profile for an "annulus" distribution.

Table 1
The Initial Parameters for All Simulations

Distribution	Embryo Mass (M_{\oplus})	$e_{ m av}$	Debris Loss	Disk Mass (M_{\oplus})
piecewise	0.025	0.05, 0.1, 0.3	25%	3, 3.25
	0.025	0.05, 0.1, 0.3	50%	4.5, 5
	0.1	0.05, 0.1, 0.3	50%	5
annulus	0.025	0.05, 0.1, 0.3	25%	2.75
	0.025	0.05, 0.1, 0.3	50%	4

Note. Masses are displayed in M_{\oplus} .

distributions. The first is modeled after the successful Hansen (2009) initial conditions, a truncated disk of embryos with a flat surface density between 0.7 and 1 au (hereafter called the "annulus"). The second disk combines this initial condition with those of Clement et al. (2021) and Clement & Chambers (2021), which both involve adding mass interior to 0.7 au (hereafter called the "piecewise"). Examples of each are shown in Figure 1. In particular, Clement & Chambers (2021) include mass with a decreasing surface density as semimajor axis decreases, and we follow this method to include embryos with decreasing surface density inward from 0.7 to 0.3 au. Most simulations are run with embryo masses of 0.025 M_{\oplus} , and we run one set with 0.1 M_{\oplus} . Total disk mass is varied for the "piecewise" distribution, and it is also increased with respect to the percentage of debris mass that is lost to collisional grinding, as discussed in Section 2.2. Table 1 lists the initial simulation parameters in more detail.

We assume an early giant-planet instability. There are currently a variety of models for the time of the giant-planet instability, but a general consensus is that one happened at some point before 100 Myr (Nesvorný et al. 2018; Clement et al. 2023b). We choose an early instability for three main reasons: its possible role in creating a truncated disk of embryos (i.e., Clement et al. 2018), to have Jupiter's secular resonances exciting embryos forming near Mercury's orbit as in Clement et al. (2021), and because of its potential to excite the embryos in the disk, causing more destructive, ironenriching collisions. As the specific evolution of the giant planets during the instability is uncertain, we take a more general approach and parameterize the eccentricity excitation to

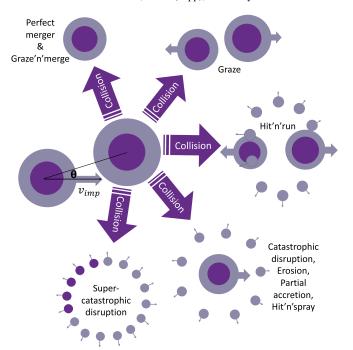


Figure 2. The nine collisional types implemented in the code are pictured here, split into their main five physical outcomes. Purple represents the core of a body, while gray represents the mantle. Large bodies are embryos, and small ones are representative of debris.

explore what level of excitation is necessary to produce Mercury's high CMF. We leave to future work the assessment of whether such a level of excitation can indeed be produced by a realistic giant-planet instability for the Solar System. The simulations begin after the instability has already occurred, and begin the simulations with a disk of embryos that have been excited by the instability. We randomly draw embryo eccentricities and inclinations from a Rayleigh distribution, varying the average eccentricity and inclination used (see Table 1 for the eccentricities and inclinations used).

2.2. Simulations

The simulations begin after the dissipation of the planetary gas disk and eccentricity excitation due to the giant-planet instability. The giant planets are thus assumed to be on their current orbits. We use a modified version of the gravitational *N*-body code Symba (Duncan et al. 1998; Scora et al. 2020). The code tracks the movement of particles within the based on gravitational interactions, and divides the particles into two categories: embryos (>2.5 × $10^{-3}M_{\oplus}$ in these simulations) and debris. Only embryos can gravitationally interact with each other; debris particles interact with the embryos but have no gravitational effect on each other. We use a time step of 3.65 days, and use a function to include the effects of general relativity on the orbits to improve their accuracy close to the Sun (Saha & Tremaine 1992).

The code uses the analytic collision prescriptions of Leinhardt & Stewart (2012), Stewart & Leinhardt (2012), and Genda et al. (2012) to calculate the outcomes of collisions between embryos. As depicted in Figure 2, collisions are divided into nine different types based on their impact energy, mass ratio, and impact angle. These can be subdivided into four main outcomes. Super-catastrophic disruption collisions are the most destructive, leaving behind only debris. Other disruptive

collisions, such as erosive collisions, and one type of grazing collision, the hit-and-spray, leave one embryo remaining and some debris, either stripped from the target or the projectile. The other grazing collisions leave behind two embryos, and possibly some debris. Finally, the merge collisions leave behind only one embryo. When debris are generated in a collision, they are limited to a maximum of 38 particles or a minimum mass of $1.5 \times 10^{-5} M_{\oplus}$ each. After each collision where debris is created, the code removes a fraction of the total debris mass created, either 25% or 50%. This mimics the effect of mass loss during and after the collisional process. The collisional grinding of debris into dust, and the subsequent loss of that dust as radiation pressure pushes it away from the Sun, is the main source (Jackson & Wyatt 2012). However, it is also possible that some of the debris mass was vapor that condensed into small, < cm-sized particles that could similarly be removed via radiation pressure or other forces (Benz et al. 2007). The amount of debris mass loss chosen for this work is somewhat arbitrary, to illustrate the effect of different debris mass-loss percentages on the outcomes. Scora et al. (2020) provide a more detailed breakdown of the collision treatment used in this code.

2.3. Composition

After the simulations are complete, we track the evolution of the embryos' compositions in post-processing following the method of Scora et al. (2020) and Scora et al. (2022). Specifically, we track the embryos' core-mass fractions (CMFs), assuming an iron core and silicate mantle. We assume that all the embryos begin completely differentiated. This is based on current work that shows small bodies can differentiate in a few million years or less (Tonks & Melosh 1992; Neumann et al. 2014; Lichtenberg et al. 2019; Carry et al. 2021), combined with work that shows collisions enhance differentiation speed (Dahl & Stevenson 2010; Rubie et al. 2015; Landeau et al. 2021), thus suggesting that our larger embryos have differentiated as they formed. For simplicity, we also assume that they have enough time to fully differentiate between collisions during our simulations, since the timescale for the cores to merge is significantly shorter than the timescale between collisions (Dahl & Stevenson 2010).

The embryos are all assigned the same initial CMF of 0.33, based on the solar Fe/Mg abundance ratio of 2.001 (Palme et al. 2014). Changes in the embryos' CMFs are tracked after each collision. The change in CMF depends on the type of collision and the initial CMFs of the colliding embryos. Figure 2 shows the basic changes that occur for each collision type. Collisions that result in perfect mergers simply result in the adding together of all the colliding material, essentially resulting in the mass-weighted average of the CMFs of the colliding bodies. On the other end of the spectrum are the highvelocity, destructive collisions such as catastrophic disruption and erosive collisions. These are the collisions where the projectile strips material off of the outside of the target embryo, resulting in a smaller embryo than at the start. The material removed is usually mantle material, so these are the collisions with the greatest potential to increase a planet's CMF. Hit-andrun collisions can also do this, but by stripping material off of the projectile instead of the target. In general, core and mantle masses are conserved when calculating the new embryo composition. The new embryo (or embryos) are assigned their changed CMFs, and the debris is made up of the remaining

core and mantle material. Core and mantle ratios are not conserved in each collisions, as a fraction of this debris material is then discarded due to debris loss. That mass is typically mantle material, since we consider that collisions strip the outer mantle material first before removing any core material. However, occasionally core material will end up in the debris, and thus sometimes core material is removed as well. More details on the specific algorithm can be found in Appendix B of Scora et al. (2020).

3. Results

3.1. Evolution of Simulations

We ran the simulations for 100 million years (Myr). In that time, they typically lost $1-2M_{\oplus}$ of mass via collisional grinding, although this left the final systems with a mass in planets $>2M_{\oplus}$, greater than that of our inner Solar System. This is because we started with 1-2.5 times the mass needed to form the terrestrial planets, as Scora et al. (2022) found that collisions could remove more than half of the initial disk mass. Based on these new results it appears we overcorrected for the amount of debris mass loss. Figure 3 shows the evolution of an "annulus" and "piecewise" simulation with a Mercury analog. In both cases, the disk of embryos and debris expands outward to larger semimajor axes over time. However, in the case of the "annulus" simulation, the embryos also extend inward, while in the "piecewise" simulation, the inner edge of embryos moves outward slightly, such that the inner edge of the disk of embryos ends up quite similar for both disk types despite the initial differences. Notice that the simulations presented in the figure both start with an average eccentricity of 0.3, which leads to multiple high-CMF bodies in the intermediate stages, yet a planet with CMF > 0.7 survives to the final system in only one of these two simulations.

In all simulations, the mass-averaged eccentricity tends to converge on $\sim 0.15-0.2$ in the first few Myr, and it tends to stagnate at this level for much of the system's evolution. Thus, the effect of the initial eccentricity is mainly confined to the first few Myr. For those simulations that start with an average eccentricity of 0.05, this means that in the first few Myr the system has fewer collisions and those happen at much lower velocities, eventually resulting in a few embryos with larger masses. For simulations with an average initial eccentricity of 0.1, the average eccentricity only needs to increase slightly, and most of the initial collisions cause one or two embryos to become significantly more massive, dominating the rest of the evolution. For those simulations with the higher initial eccentricity of 0.3, those first collisions are very destructive and cause a few embryos to become smaller before the eccentricity drops enough for the collisions to become accreting. Overall, these simulations have more of the most destructive collisions (e.g., super-catastrophic and erosion) than those with lower initial eccentricities (see Figure 4).

In general, in these simulations there are a wide variety of collision types. Collisions can have impact velocities of up to 20 times the escape velocity. In general, the most common collision type is hit-and-run, though in simulations with lower initial eccentricities, partial accretion is the most common outcome. On average, planets are the result of 37 giant collisions during the formation process, though there is a wide spread of values, anywhere from 0 up to 160 collisions per planet. More massive planets ($\geqslant 0.2\,M_{\oplus}$) have 59 collisions on

average, while small planets, unsurprisingly, form after fewer collisions, around an average of 5. We find that collisions between smaller embryos ($<0.2 M_{\oplus}$) have different frequencies of collision types than those for larger embryos ($>0.2 M_{\oplus}$). Grazing impacts, like hit-and-runs, are the most frequent collisions between small embryos, and they have higher frequencies of destructive collisions, like erosion and supercatastrophic. This is good for forming Mercury analogs, as both of these collision types are thought to be capable of forming Mercury. Meanwhile, collisions between larger embryos are strongly dominated by partial accretion collisions. This is likely due to a combination of the higher escape velocity that larger embryos have, which reduces the $v_{\rm imp}/v_{\rm esc}$ ratio and thus results in less destructive collisions, and the fact that the larger embryos have a larger effective cross section, which results in more head-on collisions.

We expected that the ν_5 secular resonance with Jupiter around 0.35 au would result in debris and other material getting absorbed by the Sun (and therefore ejected from the system), as the resonance would destabilize the bodies, thus allowing for less debris reaccretion where Mercury forms. Figure 5 shows the distribution of mass ejected from the system as a function of its semimajor axis; there is indeed a peak in mass loss near 0.35 au, more prominent in the "piecewise" simulations than in the "annulus" simulations, due to the increased mass present at those locations. However, there is not enough mass lost near 0.35 au to deplete the inner disks down to a few times Mercury's mass. Thus, the impact of the ν_5 resonance was not as strong as expected, or there are other factors at play that replenish the mass lost at the inner edge of the disk. In both types of simulations, there are also peaks in the mass ejected around 1.5 au, and between 2 and 2.5 au for both types of initial conditions. The outer peak is due to a number of resonances with the giant planets (i.e., ν_5 , ν_6 , and the 3:1 meanmotion resonance with Jupiter (Moons & Morbidelli 1995; Michel & Froeschlé 1997; Gladman et al. 2000)). The ν_5 resonance is also present at higher inclinations at the peak near 1.5 au (Michel & Froeschlé 1997; Fenucci et al. 2023). Since these disks start out with a wide range of inclinations, these resonances still have a significant effect in this area. Additionally, a number of small, eccentric embryos tend to be ejected from the main disk and end up near 1.5 au, exciting each other and the surrounding debris. This both ejects debris and embryos on its own and increases the number of bodies affected by the ν_5 resonance at higher inclinations. Conversely, bodies excited by the ν_5 resonance may then be ejected via close encounters with the embryos in the area.

3.2. Dynamical Solar System Analogs

We identify our Solar System planet analogs using criteria similar to those of other studies in the field (e.g., Lykawka & Ito 2019; Clement et al. 2021). The analogs in this section are identified as follows:

- 1. A Mercury analog lies at a semimajor axis between 0.25 and 0.5 au, and has a mass between 0.025 and 0.25 M_{\oplus} .
- 2. Earth and Venus analogs lie between 0.5 and 1.3 au, and are above $0.6 M_{\oplus}$. If there is one analog in this space, it is an Earth analog, and a second analog is the Venus analog.
- 3. A Mars analog lies between 1.3 and 2 au, and is less than 0.3 M_{\oplus} .

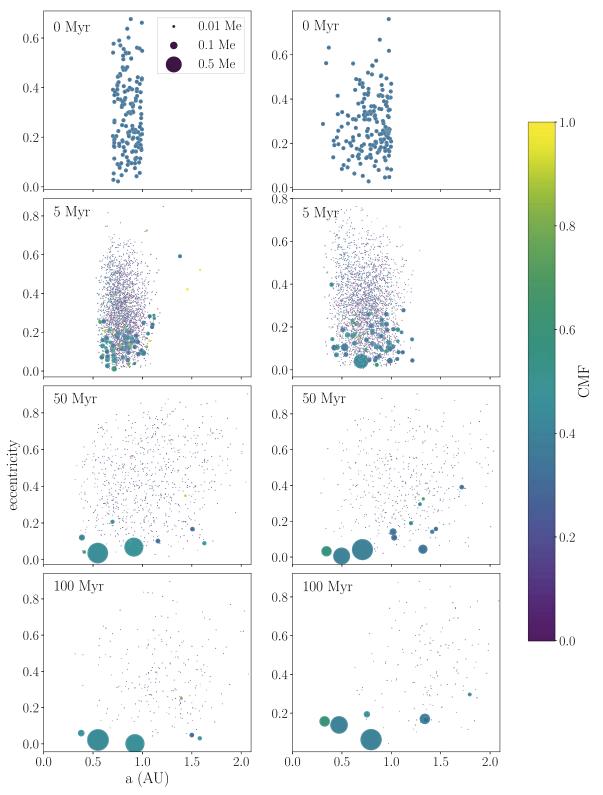


Figure 3. The evolution of sample "annulus" (left) and "piecewise" (right) simulations that form Mercury analogs. The sizes of the bodies represent their masses, and their colors represent their CMFs.

Out of our 117 simulations, 54% have at least three Solar System analogs, and only 11% have analogs of all four Solar System planets. Figure 6 shows a few of the best Solar System analogs out of our simulated systems. Most synthetic solar systems have additional mass outside of the Solar System planet analogs, both in additional planets and also in debris.

The average number of planets per simulation is 6.5, higher than the four we aim for. Typically, these extra planets are Mars analogs. In these simulations, we consider a planet to be any body that is above the minimum embryo mass in the simulation, which is $2.5 \times 10^{-3} M_{\oplus}$. The excess total mass in our results compared to that of the terrestrial planets is due to

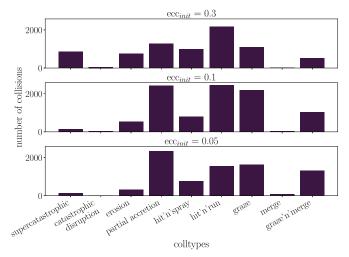


Figure 4. The collision frequencies for each collision type, for simulations with respective average initial eccentricities of 0.3 (top), 0.1 (middle), and 0.05 (bottom). Hit-and-run and partial accretion collisions are most common. Erosion collisions become more common as the average initial eccentricity increases.

the large initial mass we assumed, but this can presumably be adjusted by starting with a less massive disk.

Figure 7 shows the mass and semimajor axis distribution of planets across all of our simulations, compared to the Solar System planets. Overall, we approximately reproduce the distribution, similar to previous works, and more importantly, we achieve the appropriate masses and semimajor axes for Mercury analogs. Just over 26% of systems have a Mercury analog in mass and semimajor axis. There is a significant tail of planets near Mars, which is due to the fact that simulations tend to have multiple Mars analogs in a system instead of just one. However, these often also have high eccentricities, and so may be ejected given long enough simulation time. We ran a few simulations for longer in order to test their long-term stability. In these runs, Mars analogs tended to decrease in number, in particular in runs with many of them. In addition, $\sim 15\%$ of the dynamical Mercury analogs in those simulations were lost. This adds further weight to the idea of unstable Mercury analogs as discussed in Section 3.4. However, due to the length of time required to continue these simulations beyond 100 Myr, a full analysis of the long-term stability of these planetary systems is outside the scope of this work.

The distribution in Figure 7 also skews toward higher masses than expected for the Solar System, and at smaller semimajor axes. In particular, Venus analogs tend to be more massive and closer to the Sun than expected. This is in large part due to an excess of initial mass in the inner disk portion, and is therefore more pronounced in runs with the initial "piecewise" disk distribution. However, those with the typical "annulus" also have Venus and Earth analogs that are too close to the Sun, as seen in Figure 7, indicating that the initial distribution does not completely account for the mismatch. We discuss this further in Section 4.2.

An additional result of the Venus analogs forming too close to the Sun is that Venus and Mercury tend to form too close together. This is a consistent issue in formation simulations of the Solar System, as mentioned in Section 1, and our systems are no exception. The majority of systems have period ratios of Venus analogs to Mercury analogs below the Solar System

value of 2.55. A handful of systems have a similar value to the Solar System, and some have an even higher value. However, most of those with a higher period ratio also have an additional body that has formed between Venus and Mercury.

3.3. Mercury Analogs

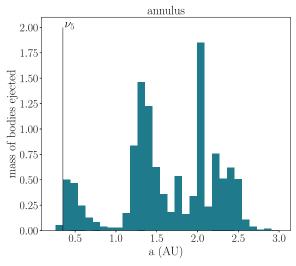
Our dynamical criteria for a Mercury analog are described above, in Section 3.2. We also consider various minimum CMFs for a Mercury analog, since Mercury's CMF is thought to be ~ 0.7 (Hauck et al. 2013). Figure 8 shows all surviving Mercury analogs with a CMF above 0.4. This reduces the Mercury occurrence rate from 26% to 10%. These analogs tend to be more massive than Mercury, and are mostly found between 0.3 au and Mercury's orbit (0.38 au). Only four of these Mercuries have a CMF above 0.5 (plotted above in Figure 8), so increasing the minimum CMF to 0.5 drops the Mercury occurrence rate to \sim 3%. We do not get any Mercury analogs with a CMF of ~0.7. One additional constraint we consider is the difference between the CMF of Earth and Mercury. In the Solar System, Earth's CMF is ~ 0.326 (Stacey 2005), less than half of Mercury's CMF. Only two of our simulations have both a Mercury and an Earth analog where the Mercury's CMF is 1.5 times that of the Earth, and both of them are simulations where the Mercury analog's CMF

Mercuries (with a CMF > 0.4) form with a slightly higher occurrence rate in the "piecewise" simulations (11%) than in the "annulus" simulations (8%), though this difference is so small that it is statistically insignificant. However, three of the four Mercuries with CMF > 0.5 are from "piecewise" simulations, which suggests that these simulations are better at forming Mercuries with higher CMFs. Mercury analogs also seem evenly spread across simulations with different initial eccentricities and inclinations. They form more frequently in simulations with 50% debris loss and therefore higher disk masses. On average, these Mercury analogs have eccentricities of 0.15.

Mercury analogs have a variety of histories. The two smallest formed after having been the second-largest remnant in two or more hit-and-run collisions. This is one of the most prevalent theories for Mercury's collisional history (Asphaug & Reufer 2014; Chau et al. 2018; Jackson et al. 2018). Thus, this does seem to be the best way to form a high-CMF, low-mass Mercury, though it does not appear to be very common in our simulations. The other Mercuries form from a variety of collisions, but typically at least one erosion collision and often a few hit-and-runs, although they are often the largest remnant in these collisions.

3.4. Proto-Mercury Analogs

In order to get a better sense of how Mercuries form, and their survival rate, we track the formation and fates of proto-Mercuries across our simulations. The criteria we set for a body to be a proto-Mercury follows the dynamical criteria for a Mercury analog as described in Section 3.2. We require a minimum CMF of 0.4, as in Section 3.3. Finally, we place some limits on the duration of the proto-Mercury's existence (i.e., the length of time that it meets the above criteria), and the time by which the proto-Mercury has formed. For the former, we require it to exist for a minimum of 5 Myr. For the latter, we require that the proto-Mercury exists a minimum of 10 Myr after the start of



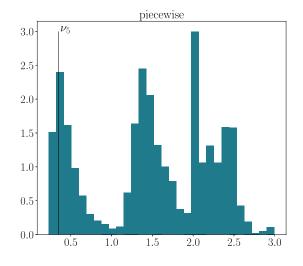


Figure 5. The total mass of bodies ejected in each semimajor axis bin for "piecewise" simulations (left) and "annulus" simulations (right). The black line shows the rough location of the ν_5 resonance. There is a peak in mass loss just to the right of this line for both simulation types.

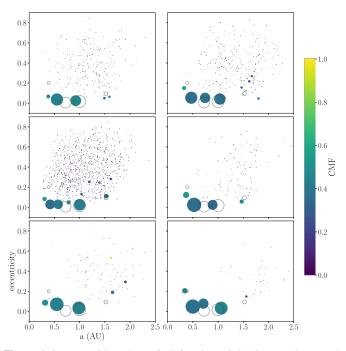


Figure 6. Systems with analogs of all four inner Solar System planets and Mercury analogs with CMF > 0.4. The size of the bodies represents their mass, and the empty circles show the locations and masses of the actual Solar System planets.

the simulation, or once the largest embryo in the simulation reaches $m_{\rm max}=0.5M_{\oplus}+m_{\rm init}$, where $m_{\rm init}$ is the initial mass of the embryos in that simulation. This is a rough approximation that the simulation has reached or is nearing the oligarchic phase, where more massive embryos dominate the evolution of the disk. This also typically corresponds to a time of 10-20 Myr, which is roughly the time by which most Mercury analogs have reached their final semimajor axis.

Including surviving Mercury analogs, 25% of our simulations have at least one proto-Mercury, and \sim 4% of the simulations have two or more proto-Mercuries that form. We also consider "dynamical" proto-Mercuries with no minimum CMF (criteria as described in Section 3.2), and find that these

form in 40% of simulations, where there are two or more proto-Mercuries in 10% of simulations. Both of these are roughly twice the occurrence rates of surviving Mercuries in our simulations. Thus, forming Mercury-like bodies is easier than keeping them in the system.

The majority of proto-Mercuries that do not survive are removed from the system after being engulfed by another body. This other body is usually either another proto-Mercury or a Venus analog orbiting further out, which in our simulations is at ~ 0.5 au. After engulfment, the other ways of "losing" a proto-Mercury include it exceeding the mass threshold, falling below the CMF threshold, or moving out of the semimajor axis limits (a > 0.5 au). The first two are the most common. In some cases, the proto-Mercury will stop being a Mercury shortly before being absorbed by another body. The problem does not seem to be forming a Mercury-like body, but rather keeping it in a stable orbit and at a high CMF.

There are some differences between Mercuries in "annulus" disks versus those in "piecewise" disks. First of all, dynamical proto-Mercuries (with no minimum CMF) are significantly more frequent in "annulus" simulations compared to "piecewise" simulations. As stated above in Section 3.3, the opposite is true for surviving Mercury analogs (though by a small amount). Thus, it may be easier to form Mercuries with the "annulus" initial conditions, but those Mercuries are also much more unstable. It makes sense that these proto-Mercuries would be unstable, because the initial disk does not extend into the range of semimajor axes allowed for Mercury, so these embryos have to be knocked inward by close encounters or a collision. However, this does not mean that all Mercury analogs in the "piecewise" disks start between 0.25 and 0.5 au. Often, "piecewise" Mercury analogs move into this range from further out in the disk, although the process is less abrupt than in the "annulus" disks, as there is a continuous distribution of material across much of these semimajor axes. An additional feature of the "piecewise" proto-Mercuries is that they have a higher probability of becoming too massive, since in these simulations the disk starts with more material in the Mercury semimajor axes, allowing for more accretion of small embryos and debris.

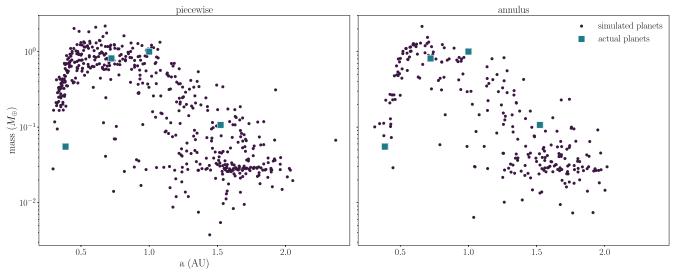


Figure 7. The masses and semimajor axes of all planets formed in our simulations, compared to the mass and semimajor axis of the four inner terrestrial planets. The distribution mostly matches the four planets for both disk types, though the inner planets are slightly too massive to include Mercury for the "piecewise" disks.

4. Discussion

4.1. Adjusting Debris Mass Loss

As discussed above in Section 3.3, our highest-CMF Mercury analogs have CMFs < 0.7, Mercury's inferred CMF (Hauck et al. 2013). The planets reach CMFs of 0.7 or higher during their formation, but other collisions and debris accretion in particular result in a decrease of the final planet's CMF, even considering that we remove 25%-50% of the debris mass formed at every collision, due to collisional grinding. However, recent work suggests that the fraction of debris lost to collisional grinding in the Solar System may be significantly higher, as high as 98%, in order to avoid overpopulating the asteroid belt with debris from collisions (S. Admane and S. A. Jacobson 2024, in preparation). A higher debris mass-loss fraction may also have a significant impact on the final CMFs of our Mercury analogs, so here we test what fraction of the debris mass has to be removed in order to elevate our Mercury analogs' CMFs to 0.7.

We calculated the fraction of the final planet's mass that came from debris, and the CMF of the debris that was accreted. Assuming that the CMF of the accreted debris remains the same, we then calculate how much debris mass has to be removed in order to increase the CMF of the final planet as close to 0.7 as possible. Roughly half of the Mercuries cannot reach a CMF of 0.7 even with removal of 100% of the debris mass they accreted. The other half can reach 0.7 CMF with an adjusted total debris mass loss spread from 60% to 98%. We also perform this calculation for those proto-Mercuries that became too massive or their CMF dropped too low, to see if this calculation would recover any of these to the point that they could be considered Mercury analogs again. We in fact find that the majority of the proto-Mercuries in these categories become Mercury analogs by our criteria set out in Sections 3.2 and 3.3, with 90%-100% total debris mass loss. Many of them do not reach a CMF of 0.7, but most of them have CMF \geq 0.4. Additionally, those proto-Mercuries that became too massive, when they lose most of the debris that was accreted, return to masses $<0.25M_{\oplus}$. With this higher rate of proto-Mercury survival, we get more than double the number of remaining Mercury analogs, an occurrence rate of 34% (see Figure 9).

This is not a perfect solution, unfortunately. We also calculate the new CMFs of the other planets in the system with this new debris mass-loss fraction that is required for the Mercuries to have a CMF of 0.7. While some planets retain their initial CMF, many of the planets in the system have accreted a large fraction of their mass from debris, and so the removal of this debris significantly increases their CMFs as well. More massive planets, such as the Venus and Earth analogs, can have CMFs as high as 0.8 or 0.9. Since the Earth's CMF is known to be 0.326, and Venus' is thought to be similar (Stacey 2005), these high debris mass-loss scenarios do not match the constraints of the whole Solar System. Thus, with this simple scaling, it seems unlikely that a higher overall fraction of debris removal in our simulations would have provided accurate Earth and Venus analogs, even if it did improve the Mercury analogs and the rate of Mercury analogs.

To that end, we considered the possibility that the debris mass-loss fraction varies with respect to the planet's semimajor axis. Watt et al. (2024) simulated the evolution of debris from giant impacts at different semimajor axes, showing that giant impacts that occur at smaller semimajor axes produce more massive debris disks via collisional grinding. Additionally, Spalding & Adams (2020) showed that the stronger solar winds likely present at the time of Mercury's formation should result in increased outward migration of debris particles, faster closer in to the Sun and slower farther out. It follows that the debris mass-loss fraction would be higher for closer-in planets like Mercury and lower for planets further from the Sun, due to the combination of these two effects. To test how this would influence the creation of Mercury analogs, we constructed two power laws to describe debris mass-loss fraction over semimajor axis. One was loosely fitted to the mass of the debris disks created at different semimajor axes in Watt et al. (2024; which we will call $P_{5,3}$), and for the other we chose a simple power law of x^{-2} (which we will call P_2).⁸ Both power laws were normalized such that they reach a maximum debris mass-loss fraction of 1 around 0.3 au, but drop off after 0.5 au. We then used both power laws to recalculate any increased

The equation used for this was $y = 1.99 \times 10^{-3} x^{-5.3}$

The equation used for this was $y = 6 \times 10^{-2} x^{-2}$

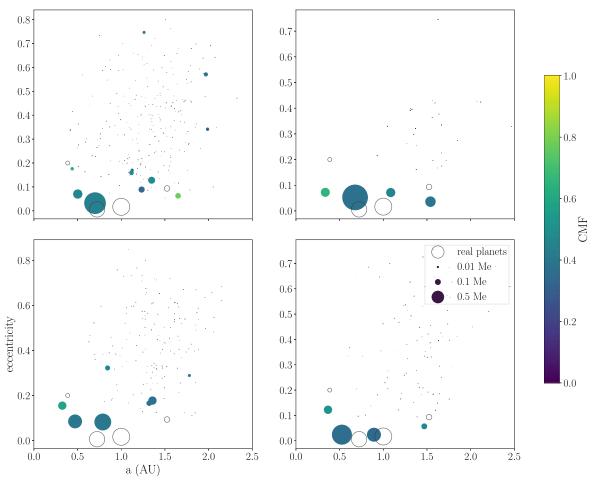


Figure 8. The systems with Mercury analogs with CMFs > 0.5. Top left is an "annulus" simulation, and the rest are "piecewise" simulations. Two are from simulations with initial average eccentricity of 0.3. The Solar System planets are represented by empty circles for comparison.

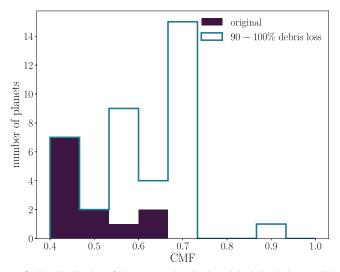
debris mass loss for each planet based on its final semimajor axis.

With the newly recalculated debris mass-loss fraction for each planet, we calculate a corresponding new mass and CMF. As might be expected, the change in planet CMF follows a slope similar to that of the debris mass-loss power laws we used, increasing exponentially for planets interior to 0.4 or 0.5 au. Unlike the previous method, this means that the analogs of the other planets remain relatively unchanged. Similarly to the above, we take this updated set of planet masses and CMFs and search for Mercury analogs. The comparison between the original distribution of Mercury analogs and those existing in the new sample is shown in Figure 9. It is clear from this figure that there is a significant increase in Mercury analogs for both power laws. For $P_{5,3}$, the rate of Mercury analogs is $\sim 27\%$, similar to when an overall debris mass-loss rate of 90%-100% is considered. For P_2 , the rate of Mercuries is similar at \sim 29%. Both are a significant increase from the 10% occurrence rate we find in the original simulations. There remains the caveat that this is just an approximation, as we assume a debris mass-loss rate based on a planet's final location, instead of its location over time. Additionally, removing debris can change the dynamical evolution in unanticipated ways. Thus, we suggest that incorporating a debris mass-loss fraction that changes with semimajor axis for giant collisions could have a significant impact on the creation of Mercury analogs in future Solar System simulations, and that this is an important avenue for future work

4.2. Debris Accretion by Inner Planets

In this study, we assume an early instability, so the giant planets start in their current positions and have their current orbital parameters. We chose this configuration so that the initial disk of embryos would start excited by this instability, and so that the giant planets would be in their current configurations, placing the ν_5 secular resonance with Jupiter near Mercury's orbit. Clement et al. (2021) found that this resonance, in combination with others, destabilized proto-Mercuries just inside of Mercury's current orbit, around 0.35 au. Thus, we hypothesized that the ν_5 resonance would similarly destabilize and eject into the Sun much of the debris created in collisions around Mercury. This would then result in reduced debris accretion near Mercury, and possibly a higher CMF for Mercury analogs.

As mentioned in Section 3.1, Figure 5 shows that there is in fact mass loss around the inner ν_5 resonance, more prominent for simulations with a "piecewise" initial condition because there is more mass near the resonance to begin with. Therefore, the ν_5 resonance seems to be actively destabilizing debris mass that then leads to its ejection. However, we do not find that the interior planets have less debris reaccretion than other planets. In fact, we find that the average fraction of a planet's mass that was accreted in debris throughout its formation period increases as its semimajor axis decreases, with the planets forming around 0.35 au (also the closest planets to the Sun that form) having the highest mass fraction of debris. This is true



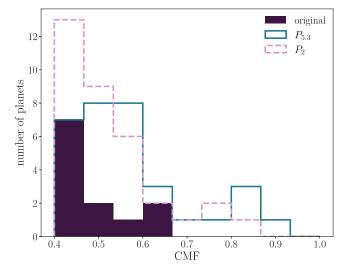


Figure 9. The distribution of Mercury analogs in the original simulations (solid purple), compared to Mercury analogs found when debris mass-loss rates are 90%–100% (left) and when debris mass loss follows two different power laws (right).

for planets with all initial conditions, including the "annulus" initial condition that starts without any mass interior to 0.7 au.

This can be attributed to a combination of factors. The first is that the Safronov number of the planets decreases as their semimajor axes decrease. The Safronov number is given by $\Theta = \frac{v_{\rm esc}^2}{2v_{\rm orb}^2}$, where $v_{\rm orb}$ is the orbital velocity of the object (Safronov 1972). It determines the fate of a planetary system where there is no significant source of damping; where this number is greater than one, close encounters tend to lead to scattering, and where it is less than one, they tend to lead to collisions (Morbidelli 2018). This therefore means that close encounters between planets and debris are more likely to be accretionary the closer they are to the Sun. Second, almost half of all debris is created inside of 0.7 au, despite the fact that all simulations begin with much less than half of their mass within 0.7 au. There is therefore a disproportionate amount of debris in the inner disk that is then available to be accreted by the interior planets. This excess of debris can be explained by the fact that, in disks of embryos with high eccentricities, the impact probability increases as the distance from the Sun decreases (Levison & Agnor 2003), and thus collisions and debris creation happen more frequently closer to the Sun. This also explains why our simulations end up with too much mass close to the Sun, where the Mercury analogs form, despite our initial distributions placing most of the mass between 0.7 and 1 au. It is also possible that some of the debris destabilized by the ν_5 resonance collides with inner planets instead of the Sun, though it seems like this would be a minor effect.

Thus, in order to better form a high-CMF Mercury, some other mechanism may be needed to more efficiently remove debris. As discussed in the Section 4.3 below, an early instability could sweep the ν_5 resonance inward through the disk, which should force more debris to be thrown toward the Sun and thus leave less to be accreted by Mercury. It is also possible that the ν_5 resonance could increase the fraction of mass loss due to collisional grinding for debris formed near this resonance, as it would bump up the eccentricities of the debris. Furthermore, collisional grinding may be more efficient closer to the Sun, as Kobayashi & Tanaka (2010) found that the mass-depletion time for collisional cascade increases with decreasing semimajor axis. This would help to remove some of the excess

debris, allowing Mercury analogs to reach higher CMFs and smaller masses. Finally, a scenario where Jupiter and Saturn start out with more eccentric orbits than their current ones would increase the strength of the secular resonances, possibly resulting in more material being removed by the inner ν_5 resonance (Raymond et al. 2009).

4.3. Comparison to Other Works

As mentioned in Section 1, some recent works have also had some success with forming Mercury analogs. Clement & Chambers (2021) formed Mercuries at a 10% occurrence rate with an inner disk of material, similar to the "piecewise" initial conditions used in this study. However, they placed Jupiter and Saturn in mean-motion resonance, on their pre-instability orbits, and tested different slopes and distributions. They also found that they formed high-CMF (>0.5 CMF) Mercury analogs around 20% of the time, which is a significantly higher rate than in our results. It seems that the treatment of collisions in the MERCURY code may be the cause. Unlike in Symba, MERCURY creates debris particles that are treated as embryos after the collision, and thus the "minimum fragment mass" is orders of magnitude larger for MERCURY (0.0055 M_{\oplus}) than it is in this study $(1.5 \times 10^{-5} M_{\oplus})$. With such large fragments, each one can make a significant difference in the CMF of the planet it accretes on. More importantly, if only one fragment is not reaccreted, this keeps the CMF of the planet much higher than it would be if only one debris particle was not reaccreted in the simulations in this work. Thus, we suggest that it is possible that the high Mercury CMFs in Clement & Chambers (2021), for example, may result from the way that debris is treated. This is not the only possible explanation, due to the other differences in the simulations of Clement & Chambers (2021; i.e., giant-planet positions). Even so, this highlights the importance of ensuring that the debris from collisions is treated as realistically as possible in planet formation simulations.

Additionally, Clement et al. (2023a) found that they form Mercury analogs frequently in their simulations, using an initial disk similar to the above, where they also simulate the early giant-planet instability and its effects on the inner terrestrial disk. In these simulations, the sweeping of the ν_5 resonance inward over the course of the formation, caused by the

instability, seemed to remove enough material in the Mercury region to form better Mercury analogs. Thus, it is possible that including such a process in our simulations may have had a similar effect, and may have reduced the debris accretion onto Mercury analogs.

5. Summary and Conclusions

In this study, we simulate the formation of the Solar System with a focus on the formation of a high-CMF Mercury. In order to facilitate Mercury's formation, we start with an inner disk of material from 0.3 to 0.7 au, attached to the typical annulus of embryos from 0.7 to 1 au, and we start with the giant planets in their current configurations. We find that 11% of simulations have an analog for each of the four inner terrestrial planets. Overall, we form too many planets per system, and specifically too many planets with high mass near 0.5 au. This is due to initial disk masses that are too large, and in particular to overly massive inner disks. These disk masses were adjusted for mass loss from the collisional grinding of debris, but less mass loss occurred than anticipated.

Mercury analogs with CMF \geqslant 0.4 form in \sim 10% of simulations, at a similar rate to recent studies with similar initial conditions (Clement & Chambers 2021). However, we fail to form Mercuries with CMFs \geqslant 0.69, which is the minimum estimate of Mercury's CMF (Hauck et al. 2013). It seems that this is due to an excess of mass and debris accretion at the inner edge of the disk, and thus one solution could be that the giant-planet instability happens during the formation period, as in Clement et al. (2023a), causing the ν_5 resonance to sweep through the inner disk and push debris toward the Sun. However, as our Mercury analogs seem to have lower CMFs than those of Clement & Chambers (2021), we also find that the implementation of debris from collisions in MERCURY may not have sufficiently high resolution to emulate the reaccretion of debris.

More generally, we draw the following conclusions from the simulations we performed:

- More proto-Mercuries form than remain in the final systems. Typically, they are removed via accretion onto other bodies in the system. This suggests that one reason for Mercury's lower occurrence rates in simulations may simply be that its formation pathway is inherently more unstable than the other planets.
- 2. Debris accretion accounts for a significant mass fraction of most planets formed, including Mercury analogs. In our work, this means that high-CMF Mercury analogs form most commonly in simulations with higher (50% instead of 25%) debris mass loss. This highlights the importance of improving our understanding of what happens to debris post-collision, and subsequently applying those improvements to our implementations of debris creation in planet formation simulations.

Our conclusions demonstrate that the most important areas of improvement for Mercury's formation still lie in the details of the collisions that form it. Additionally, they suggest that parameters that may increase the formation rate of high-CMF Mercuries may also result in lower-quality Earth analogs. Thus, a cohesive picture of the formation of all the inner planets and their compositions requires more thorough implementations of collisions and the debris they produce.

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Software:astropy (Astropy Collaboration et al. 2013, 2018), SyMBA (Duncan et al. 1998)

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